



# Introduction to quantum computing

PIERRE-EMMANUEL EMERIAU – QUANTUM ALGORITHM LEAD

POUR L'IMT ATLANTIQUE – NOVEMBRE 2024

[www.quandela.com](http://www.quandela.com)

# Overview

**1.**

A step back

→ **2.**

The basis of quantum computing

→ **3.**

A dive into quantum computing technologies

→ **4.**

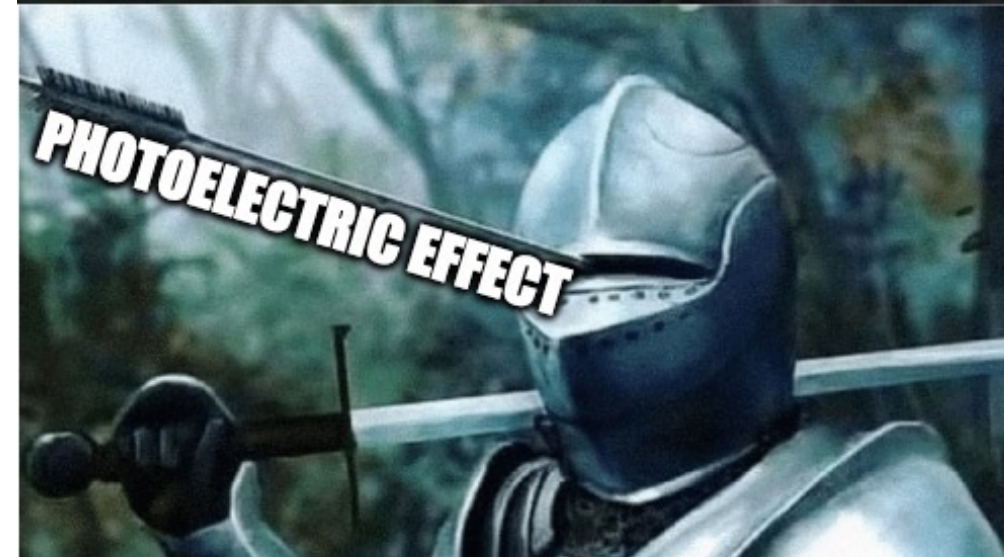
Quantum algorithms

→ **5.**

Building an idealised quantum computer

01.

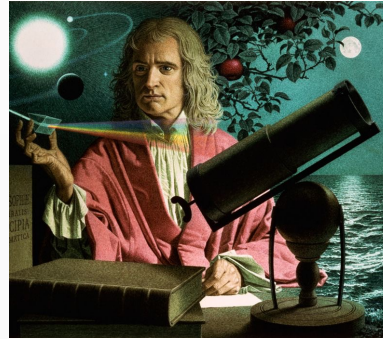
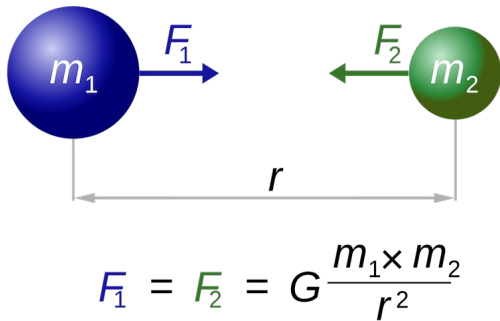
A step back



# A brief historical perspective



# A brief historical perspective



- Behavior of light (transmission, reflection, refraction, diffraction)
- Motion of objects (stars, planets, ...)
- Thermodynamics
- Electromagnetism

## Newtonian physics

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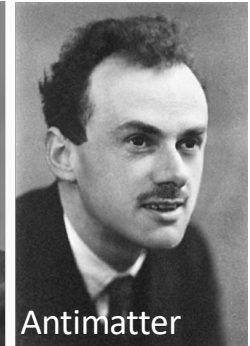
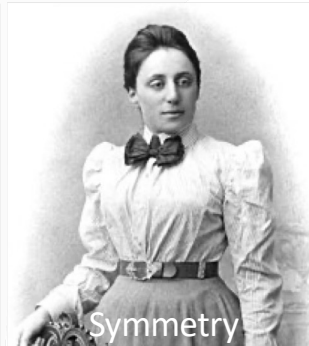
Up to 20<sup>th</sup> century

# A brief historical perspective

Weird behaviors arose...

- Black-body radiation problem
- Photoelectric effects
- ...

A need for a new 'quantised' physics

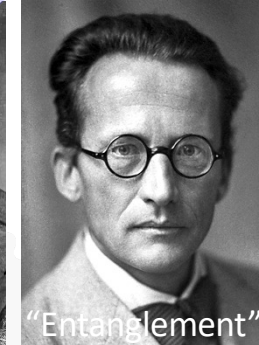


**Newtonian physics**

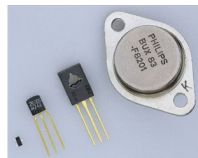
Up to 20<sup>th</sup> century

→ **Start of quantum physics**

Early 1900'



# A brief historical perspective



TRANSISTOR



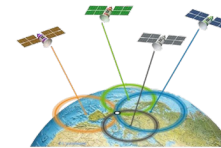
LASER



LASER DIODE



MRI



GPS



SMARTPHONES



COMPUTERS

Newtonian physics

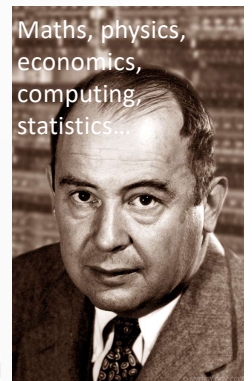
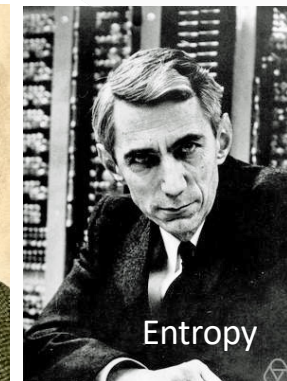
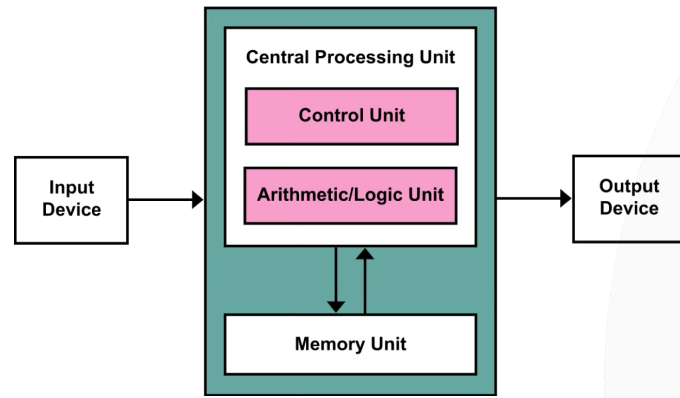
Up to 20<sup>th</sup> century

→ Start of quantum physics → 1<sup>st</sup> quantum revolution

Early 1900'

20<sup>th</sup> century

# A brief historical perspective



**Newtonian physics**

Up to 20<sup>th</sup> century

→ **Start of quantum physics** → **1<sup>st</sup> quantum revolution**

Early 1900'

20<sup>th</sup> century

**Information theory**

1940s onward



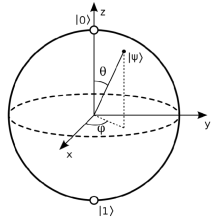
# A brief historical perspective

## SUPERPOSITION

Classical bit: 0 or 1



Quantum bit:  $\alpha|0\rangle + \beta|1\rangle$



## MEASUREMENT

$$\alpha|0\rangle + \beta|1\rangle$$



$$\text{Pr} = |\alpha|^2$$

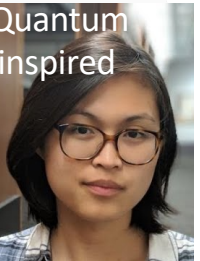
Result '0'  
State  $|0\rangle$

$$\text{Pr} = |\beta|^2$$

Result '1'  
State  $|1\rangle$

## ENTANGLEMENT

$$|\Psi\rangle = \frac{|01\rangle + |10\rangle}{\sqrt{2}}$$



Newtonian physics

Up to 20<sup>th</sup> century

→ Start of quantum physics

Early 1900'

→ 1<sup>st</sup> quantum revolution

20<sup>th</sup> century

Information theory

1940s onward

2nd quantum revolution

1980s onward

# A brief historical perspective

**Newtonian physics**

Up to 20<sup>th</sup> century

→ **Start of quantum physics** → **1<sup>st</sup> quantum revolution**

Early 1900'

20<sup>th</sup> century

**Information theory**

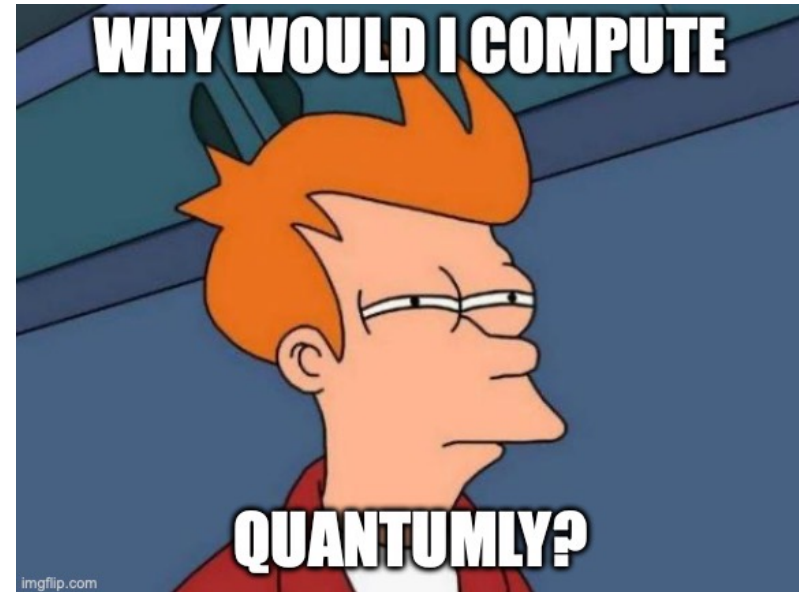
1940s onward

**2nd quantum revolution**

1980s onward

02.

## The basis of quantum computing

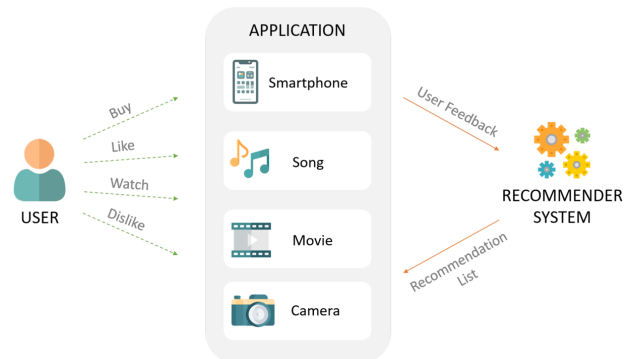


# What makes a quantum algorithm quantum?

## QUANTUM POWER? →

- Find problems where quantum computers give advantage
- Make sure new algorithms are robust to improvements in classical computing
- ~~Parallelism powers QC~~
- Where does it come from physically?
- **Highly interdisciplinary** questions

## QUANTUM RECOMMENDATION SYSTEM →



## QUANTUM RECOMMENDATION SYSTEM

QUANTUM COMPUTING

### Major Quantum Computing Advance Made Obsolete by Teenager

61 |

18-year-old Ewin Tang has proven that classical computers can solve the “recommendation problem” nearly as fast as quantum computers. The result eliminates one of the best examples of quantum speedup.



# Cooking a quantum algorithm: the basic ingredients



## SUPERPOSITION

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If a system can be in state A or state B, it can also be in a “**mixture**” of the two states. If we measure it, we see either A or B, probabilistically.

## ENTANGLEMENT

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There exist systems of multiple parts which cannot be described only in terms of their constituent parts.

It is sustained by **coherence** and leads to **non-locality**.

## COLLAPSE

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Any further measurements will give the same result.

## UNCERTAINTY

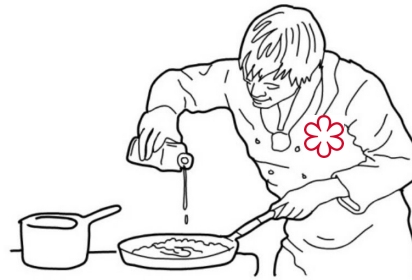
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There are pairs of measurements where greater certainty of the outcome of one measurement implies greater uncertainty of the outcome of the other measurement.

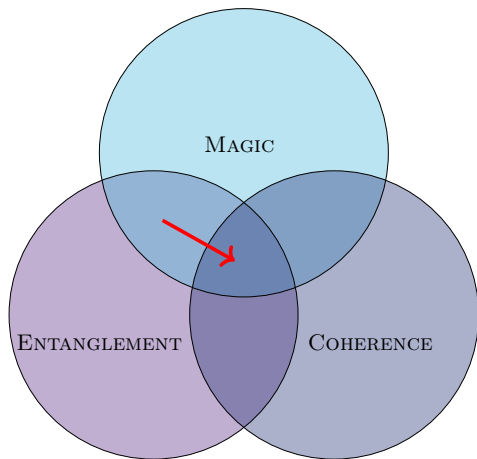
The basic idea behind quantum computing is to **use these effects to our advantage** when **processing information** encoded onto **quantum systems**



# Cooking a quantum algorithm: the chef ingredients



Resource theory!



## ENTANGLEMENT

There exist systems of multiple parts which cannot be described only in terms of their constituent parts.

## COHERENCE

Ability to keep the quantum information.

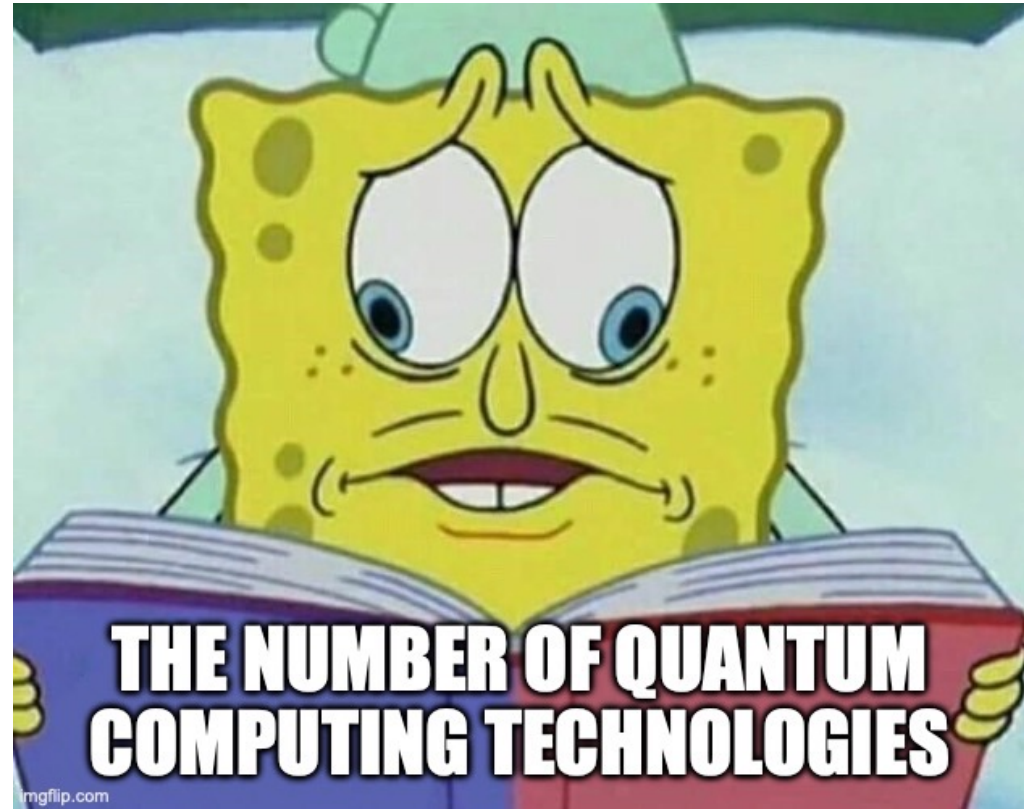
## MAGIC

Outside of stabiliser theory.



03.

A dive into  
quantum  
computing  
technologies



## The Physical Implementation of Quantum Computation

David P. DiVincenzo

*IBM T.J. Watson Research Center, Yorktown Heights, NY 10598 USA*  
(February 1, 2008)

After a brief introduction to the principles and promise of quantum information processing, the requirements for the physical implementation of quantum computation are discussed. These five requirements, plus two relating to the communication of quantum information, are extensively explored and related to the many schemes in atomic physics, quantum optics, nuclear and electron magnetic resonance spectroscopy, superconducting electronics, and quantum-dot physics, for achieving quantum computing.

DiVincenzo, David P. (2000-04-13). "The Physical Implementation of Quantum Computation". *Fortschritte der Physik*. 48 (9–11): 771–783.



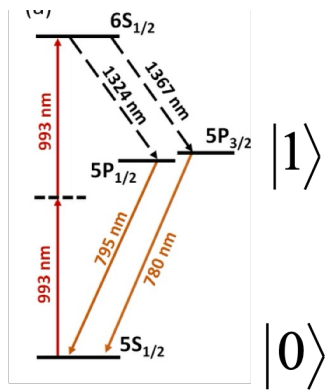
## THE DIVICENZO CRITERIA



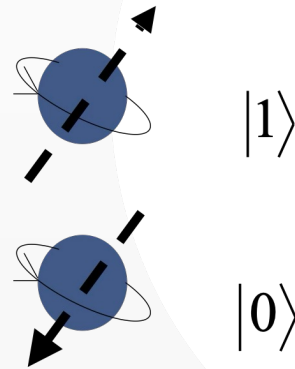
1. A **scalable** physical system with **well characterized qubits**
2. The ability to **initialize** the state of the qubits
3. **Long decoherence times**
4. A "**universal**" set of quantum gates
5. A qubit-specific **measurement capability**



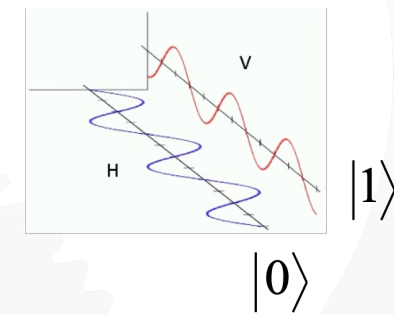
# 1. A scalable physical system with well characterized qubits



ATOM + ENERGY LEVELS



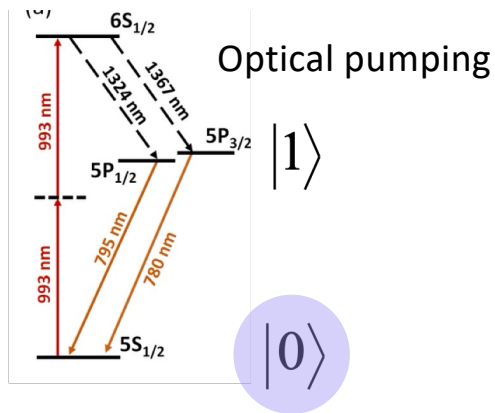
ELECTRON + SPIN



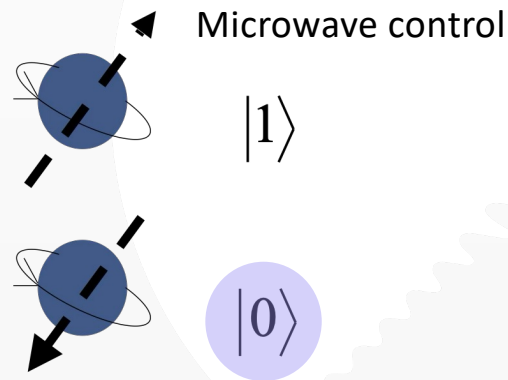
PHOTON + POLARISATION



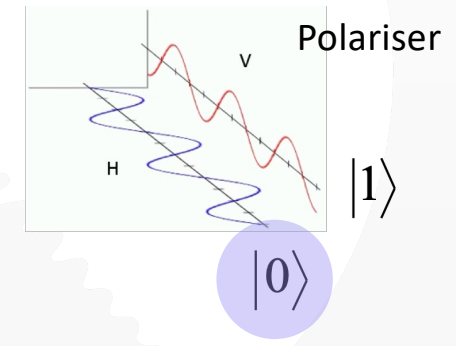
## 2. The ability to initialize the states of the qubits



ATOM + ENERGY LEVELS



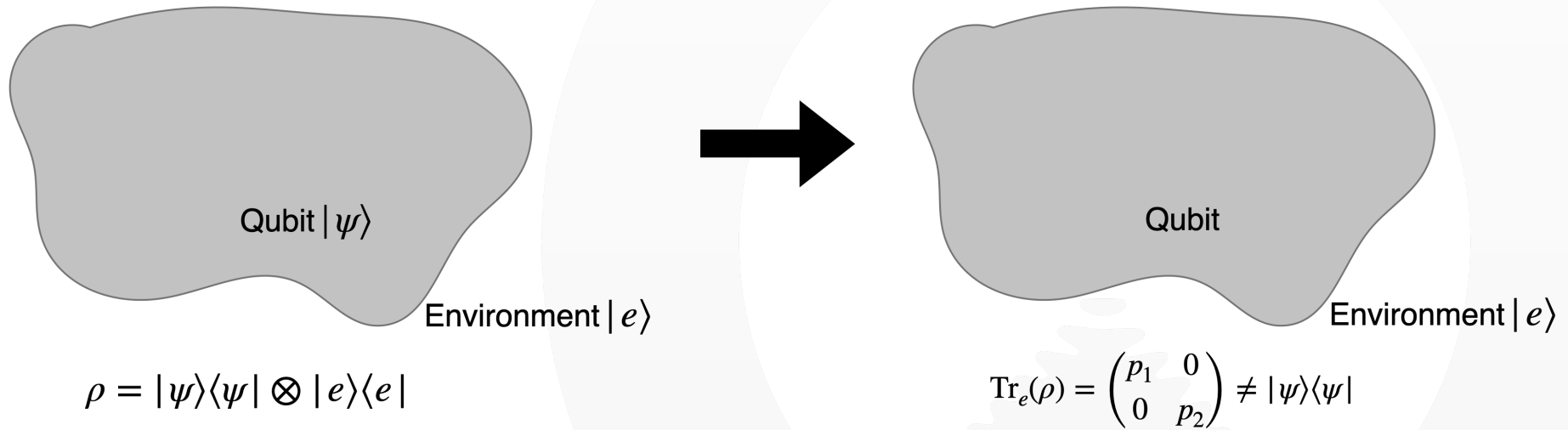
ELECTRON + SPIN



PHOTON + POLARISATION



### 3. Long decoherence times



**DIFFICULTY:**

We need isolated qubits to avoid decoherence

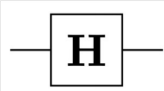
**BUT**

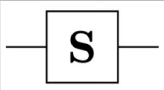
We need interactions to control the qubits and make them interfere



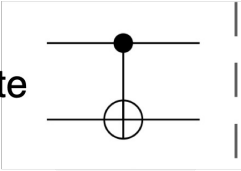
# 4. A universal set of quantum gates

Universal = can implement any unitary transformation  $\Rightarrow$  *continuous!*

Hadamard   $|0\rangle \rightarrow (|0\rangle + |1\rangle)/\sqrt{2}$   
 $|1\rangle \rightarrow (|0\rangle - |1\rangle)/\sqrt{2}$

S gate   $|0\rangle \rightarrow |0\rangle$   
 $|1\rangle \rightarrow i|1\rangle$

T gate   $|0\rangle \rightarrow |0\rangle$   
 $|1\rangle \rightarrow e^{i\pi/4}|1\rangle$

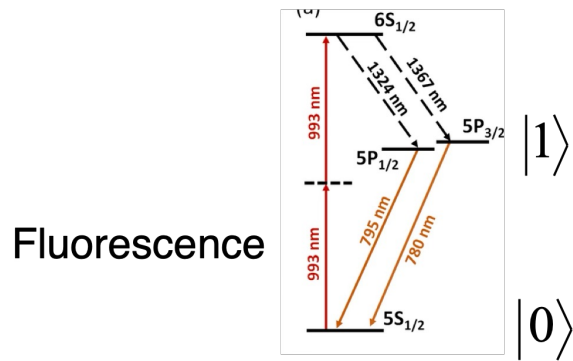
C-NOT gate   $|00\rangle \rightarrow |00\rangle$   
 $|01\rangle \rightarrow |01\rangle$   
 $|10\rangle \rightarrow |11\rangle$   
 $|11\rangle \rightarrow |10\rangle$

$\Rightarrow$  **3 SINGLE QUBIT GATES + 1 TWO-QUBIT GATE = APPROXIMATE ALL UNITAIRES**

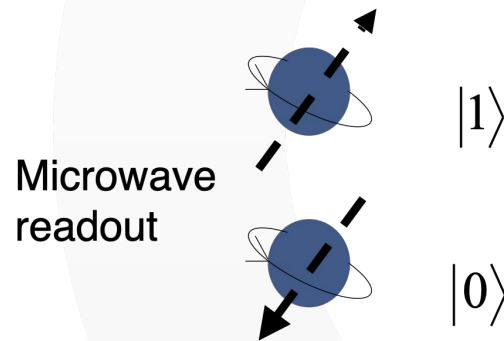


# 5. A qubit-specific readout capability

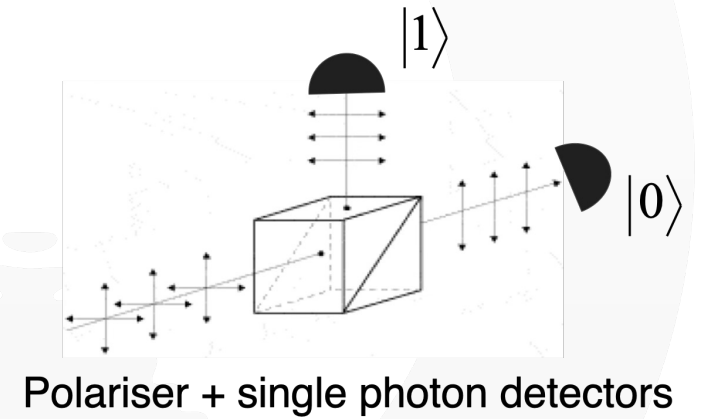
—————  $|1\rangle$   
or  
—————  $|0\rangle$  ?



**ATOM + ENERGY LEVELS**



**ELECTRON + SPIN**



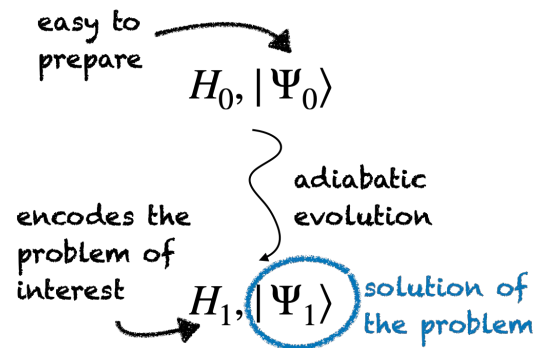
**PHOTON + POLARISATION**



# Models of quantum computation

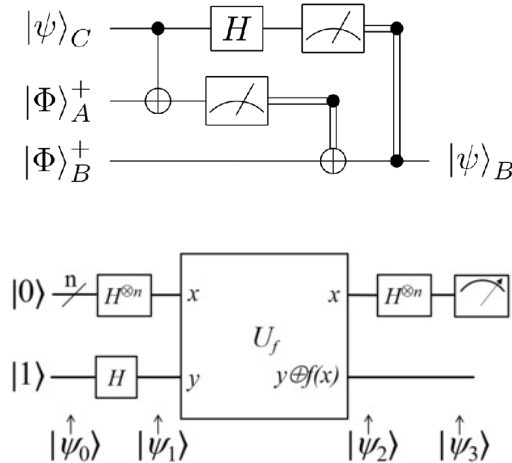
## ANALOG

### ADIABATIC



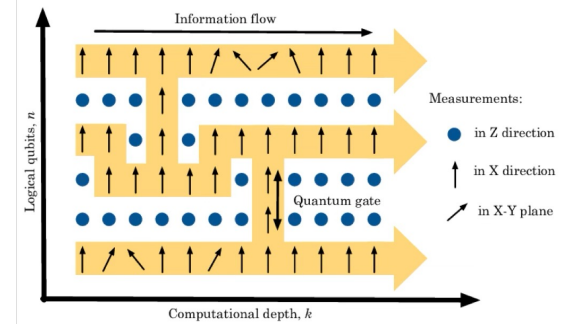
## DIGITAL

### GATE-BASED



## DIGITAL

### MEASUREMENT-BASED



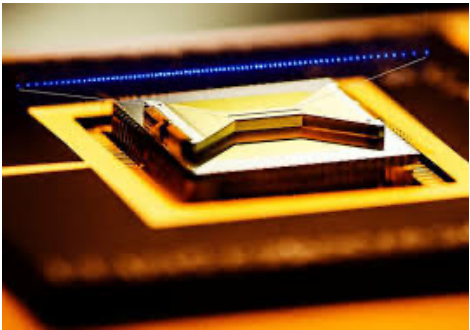
PHYSICAL REVIEW A 68, 022312 (2003)

### Measurement-based quantum computation on cluster states

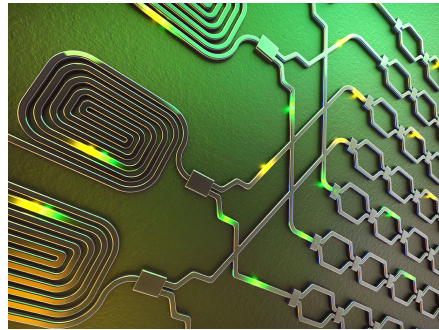
Robert Raussendorf, Daniel E. Browne,\* and Hans J. Briegel  
 Theoretische Physik, Ludwig-Maximilians-Universität München, München, Germany  
 (Received 18 February 2003; published 25 August 2003)



# Main physical implementations of a quantum computer



TRAPPED IONS



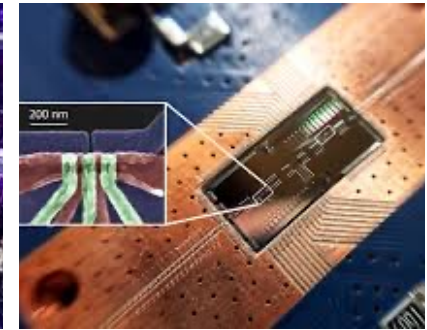
PHOTONS



SUPERCONDUCTING  
QUBITS



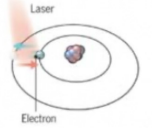
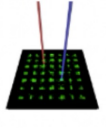
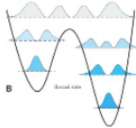
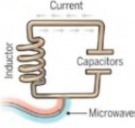

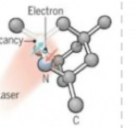
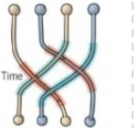
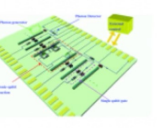














NEUTRAL ATOM



SILICON QUBITS



# Main physical implemenations of a quantum computer

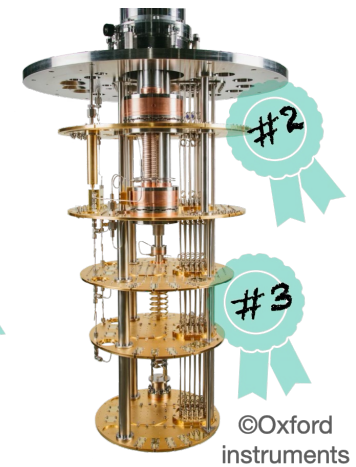
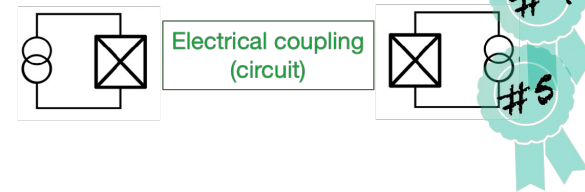
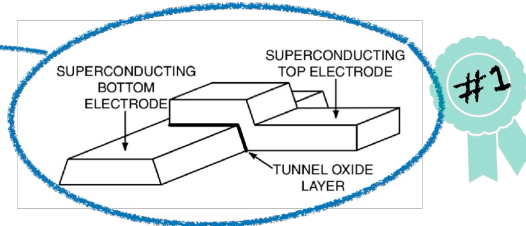
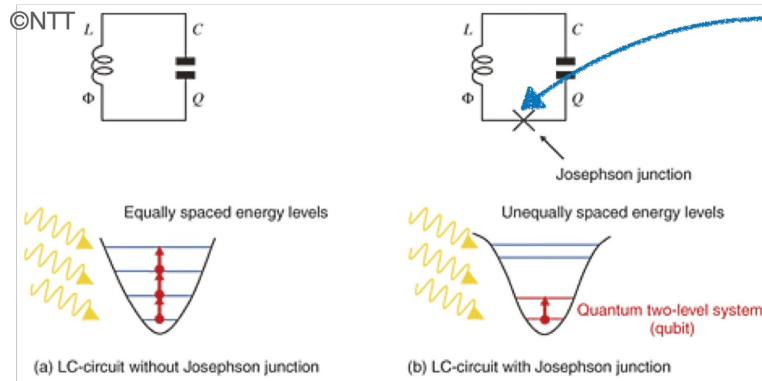
	atoms	electron superconducting loops & controlled spin				photons		
	 <p>trapped ions</p>	 <p>cold atoms</p>	 <p>quantum annealing</p>	 <p>super-conducting</p>	 <p>silicon</p>	 <p>NV centers</p>	 <p>topological</p>	 <p>photons</p>
vendors								
labs (*)			 <p>(*) non exhaustive inventory, missing Chinese labs among others</p>					

(cc) Olivier Erratty, December 2021





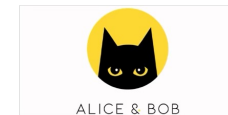
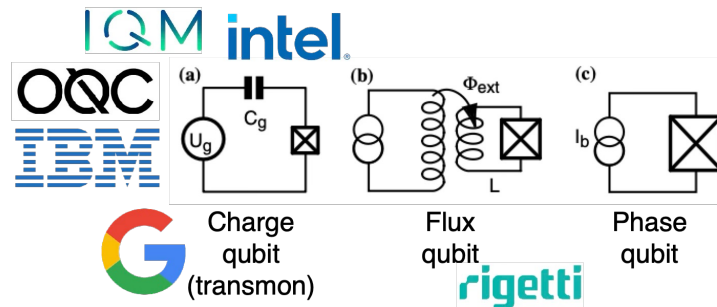
# SUPERCONDUCTING QUBITS



*Quantum Information Processing, Vol. 3, Nos. 1-5, October 2004 (© 2004)*

**Implementing Qubits with Superconducting Integrated Circuits**

Michel H. Devoret<sup>1,4</sup> and John M. Martinis<sup>2,3</sup>



# SUPERCONDUCTING QUBITS



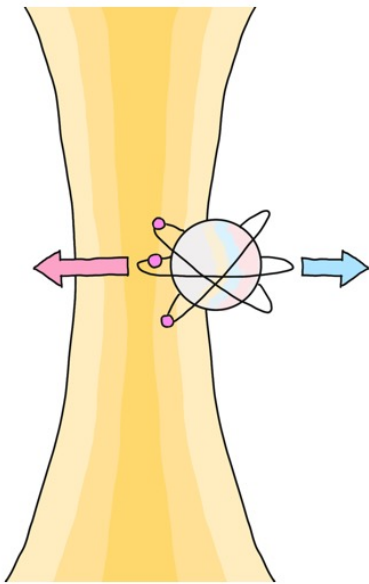
- Eletronics
- Easy and fast to control
- Several degrees of freedom



- Cryogeny (mK)
- Correlated noise
- Decoherence
- Wiring and connectivity

# NEUTRAL ATOMS

Optical tweezers

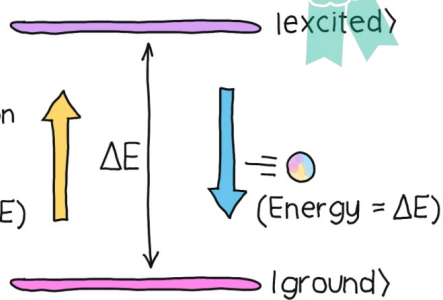


#1

photon  
≡ ●  
(Energy =  $\Delta E$ )

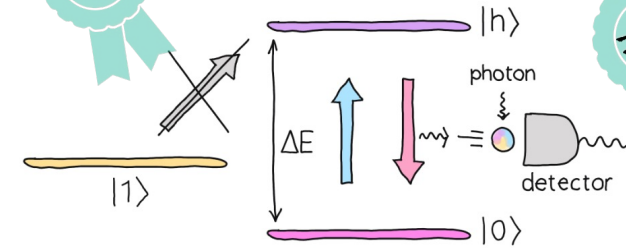
Rydberg atoms (rubidium85,...)

#3



#2

Laser cooling and fluorescence



#5

Drive hamiltonian with pulses and Rydberg blockade (Van der Waals interaction)

#4



# NEUTRAL ATOMS



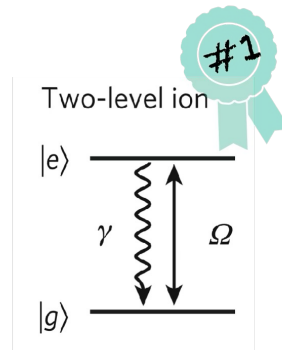
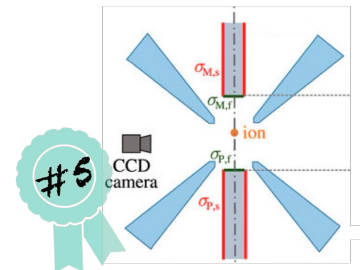
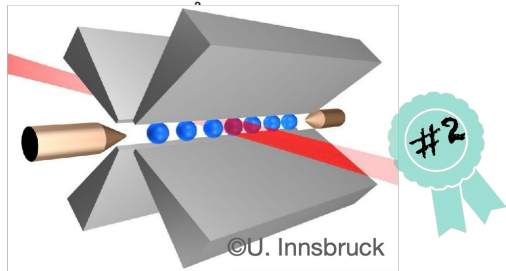
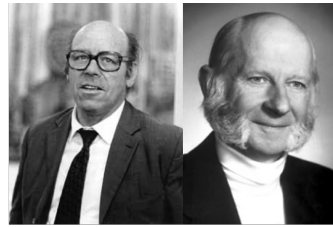
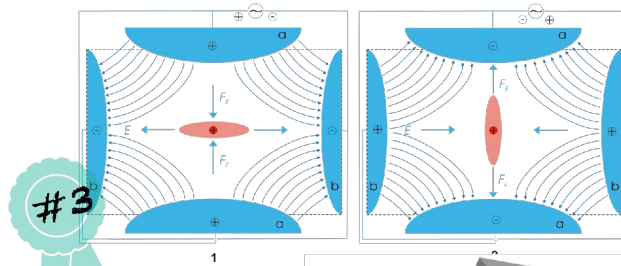
- Connectivity
- 4K to room temperature
- Great isolation



- Scalability
- Clock time

BACK TO DIVICENZO CRITERIA

# TRAPPED IONS

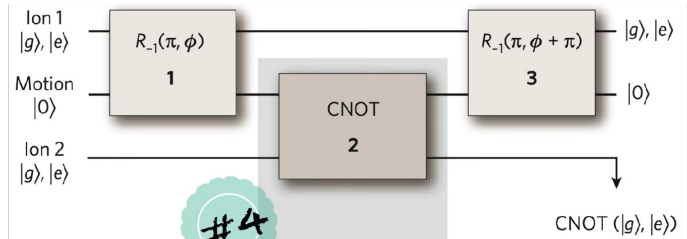


VOLUME 74, NUMBER 20      PHYSICAL REVIEW LETTERS      15 MAY 1995

**Quantum Computations with Cold Trapped Ions**

J. J. Cirac and P. Zoller\*

*Institut für Theoretische Physik, Universität Innsbruck, Technikerstrasse 25, A-6020 Innsbruck, Austria*  
(Received 30 November 1994)



# TRAPPED IONS

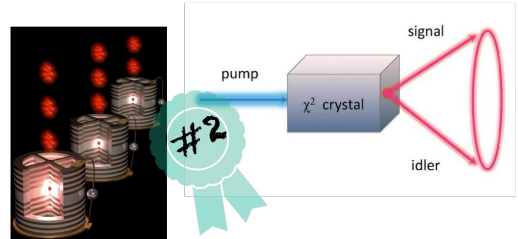
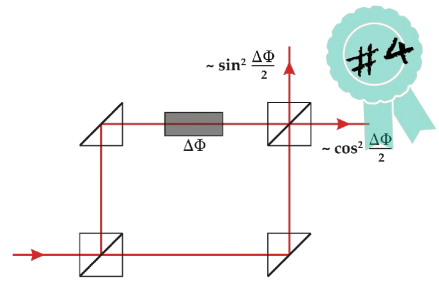
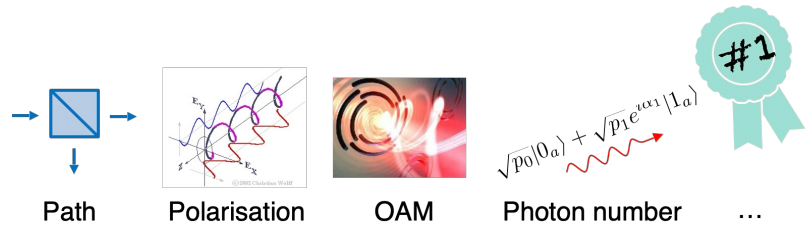


- Long coherence
- Connectivity
- 4K to room temperature
- Great isolation



- Scalability (1D)
- Size
- Clock time

# PHOTONS



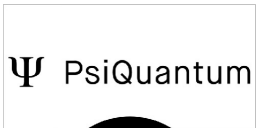
## A scheme for efficient quantum computation with linear optics

E. Knill, R. Laflamme & G. J. Milburn

Nature 409, 46–52 (2001) | [Cite this article](#)

38k Accesses | 4127 Citations | 57 Altmetric | [Metrics](#)

### DISCRETE VARIABLE



### CONTINUOUS VARIABLE



# PHOTONS



- Long coherence
- Connectivity
- 4K to room temperature
- Connection with network
- Single-qubit gates
- Modularity



- Photon loss
- Source efficiency
- Two-qubit gates



04.

# Quantum algorithms



BACK TO HISTORY

# The dawn of quantum algorithmic

1982 RICHARD FEYNMAN →



If you want to make a simulation of nature, you'd **better make it quantum mechanical**, and by golly it's a wonderful problem, because it doesn't look so easy.



1985 DAVID DEUTSCH →



Computing devices resembling the **universal quantum computer** can, in principle, be built and would have many remarkable properties **not reproducible by any Turing machine.**



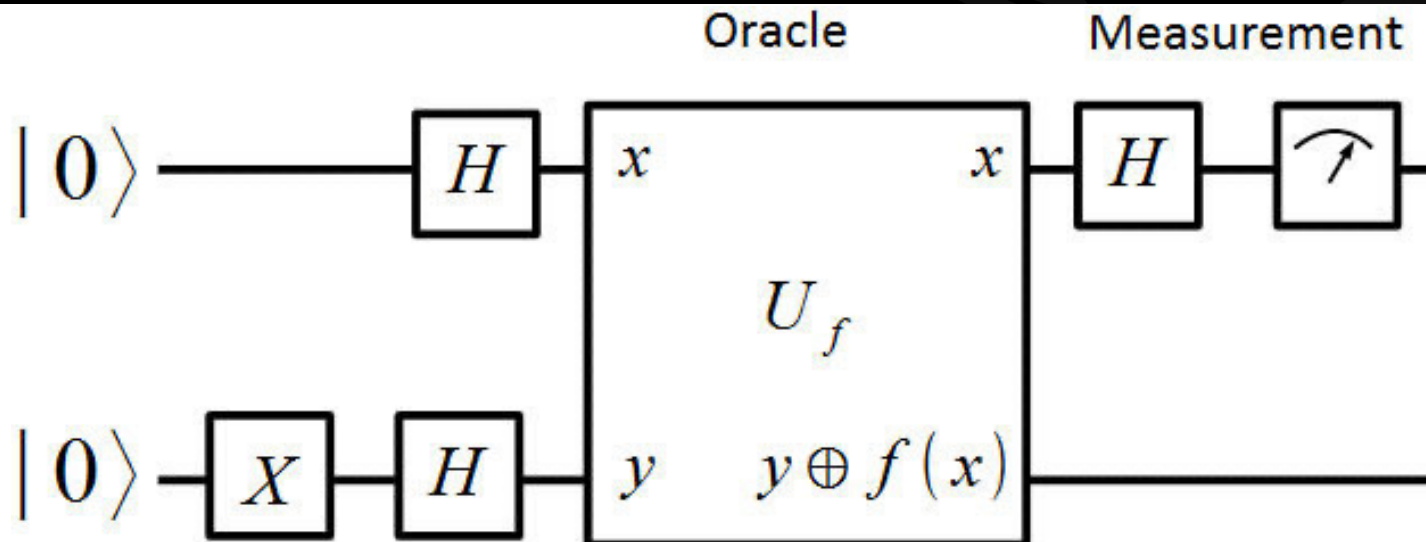
1992 DAVID DEUTSCH AND RICHARD JOZSA →



The quantum computation solves the problem with certainty **in exponentially less time** than any classical deterministic computation.

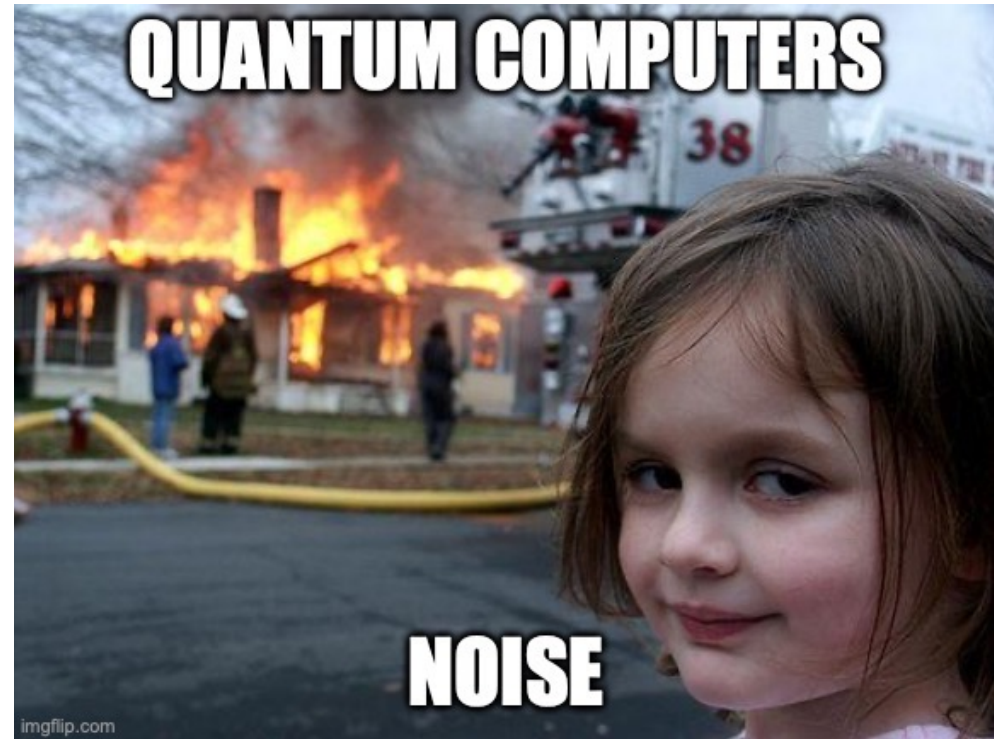


# Exercise: the Deutsch algorithm

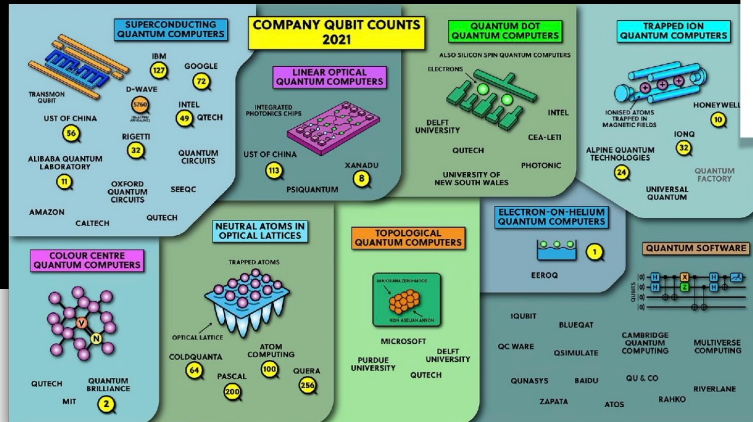


05.

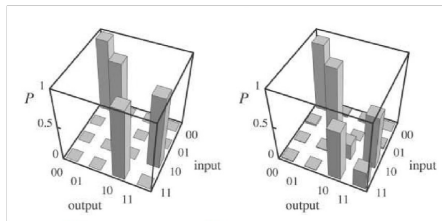
Building an  
idealised  
quantum  
computer



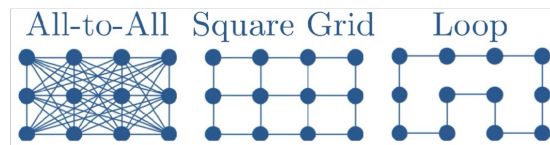
# Benchmarking quantum computers



NUMBER OF QUBITS



1- AND 2-QUBIT GATE ERROR



CONNECTIVITY

## Assessing the quality of near-term photonic quantum devices

Rawad Mezher and Shane Mansfield

Quandela SAS, 7 Rue Léonard de Vinci, 91300 Massy, France

## Characterizing quantum supremacy in near-term devices

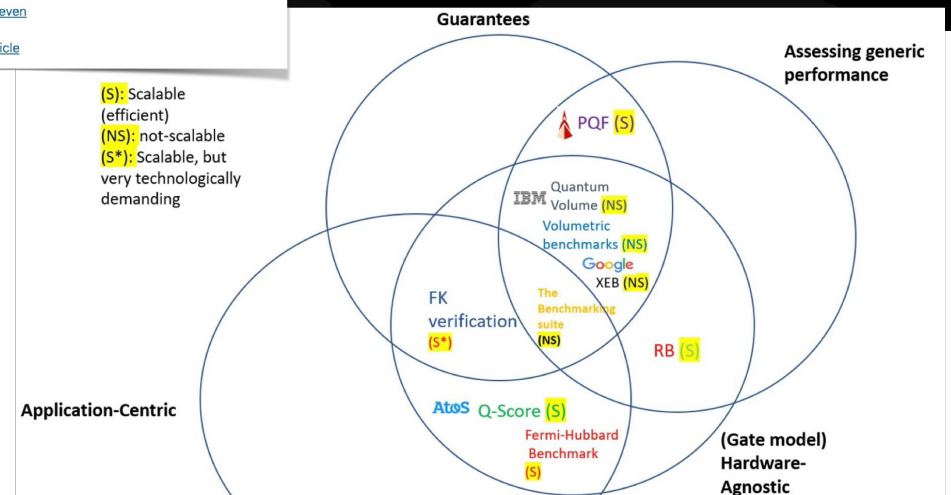
Sergio Boixo, Sergei V. Isakov, Vadim N. Smelyanskiy, Ryan Babbush, Nan Ding, Zhang Jiang, Michael J. Bremner, John M. Martinis & Hartmut Neven

*Nature Physics* 14, 595–600 (2018) | [Cite this article](#)

PHYSICAL REVIEW A 100, 032328 (2019)

## Validating quantum computers using randomized model circuits

Andrew W. Cross, Lev S. Bishop, Sarah Sheldon, Paul D. Nation, and Jay M. Gambetta  
IBM T. J. Watson Research Center, Yorktown Heights, New York 10598, USA



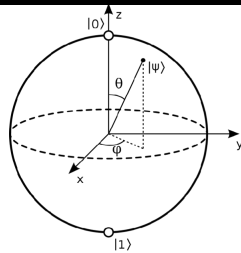
METRICS



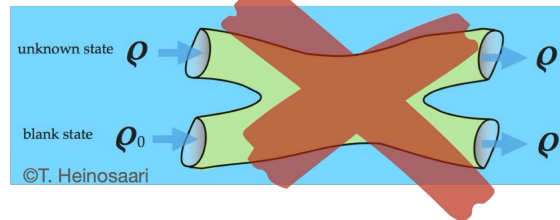
# The noise: the main issue of quantum computing

## CONTINUOUS ERRORS

Quantum bit:  $\alpha |0\rangle + \beta |1\rangle$

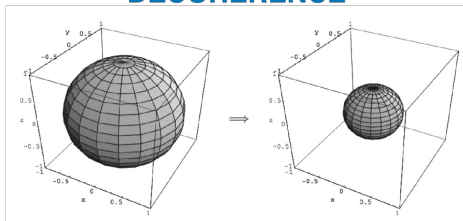


## NO CLONING

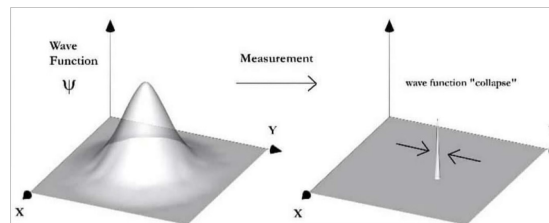


©T. Heinosari

## DECOHERENCE



## MEASUREMENT COLLAPSE



## QUANTUM COMPUTING: DREAM OR NIGHTMARE?

The principles of quantum computing were laid out about 15 years ago by computer scientists applying the superposition principle of quantum mechanics to computer operation. Quantum computing has recently become a hot topic in physics, with the recognition that a two-level system can be presented as a quantum bit, or "qubit," and that an interaction between such systems

Recent experiments have deepened our insight into the wonderfully counterintuitive quantum theory. But are they really harbingers of quantum computing? We doubt it.

Serge Haroche and Jean-Michel Raimond

two interacting qubits: a "control" bit and a "target" bit. The control remains unchanged, but its state determines the evolution of the target: If the control is 0, nothing happens to the target; if it is 1, the target undergoes a well-defined transformation. Quantum mechanics admits additional options. If the control is in some coherent superposition of 0 and 1, the output of the gate is



# Short to mid term: error mitigation

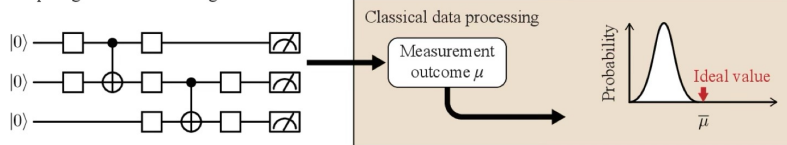
PHYSICAL REVIEW X 8, 031027 (2018)

## Practical Quantum Error Mitigation for Near-Future Applications

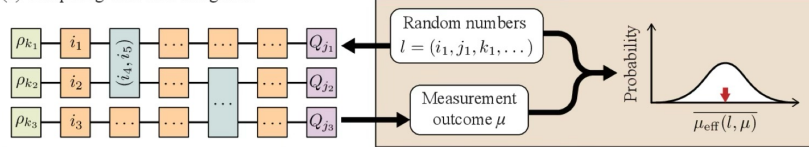
Suguru Endo,<sup>1</sup> Simon C. Benjamin,<sup>1</sup> and Ying Li<sup>2,1,\*</sup>

<sup>1</sup>Department of Materials, University of Oxford, Oxford OX1 3PH, United Kingdom  
<sup>2</sup>Graduate School of China Academy of Engineering Physics, Beijing 100193, China

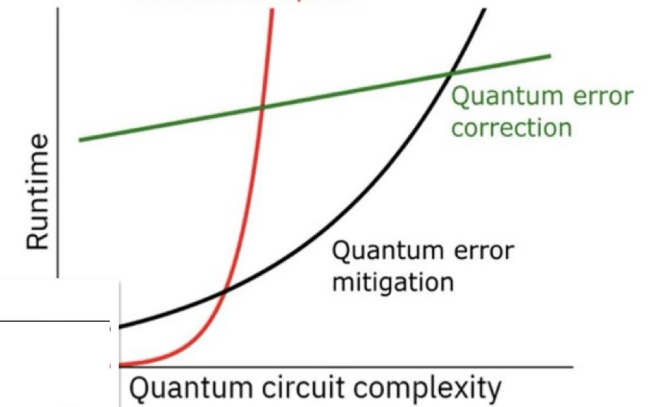
(a) Computing without error mitigation



(b) Computing with error mitigation



Classical computer

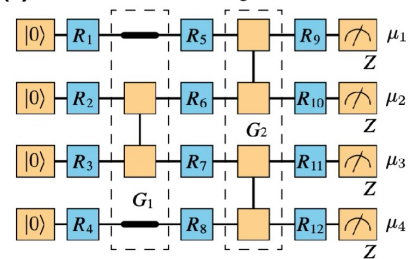


PRX QUANTUM 2, 040330 (2021)

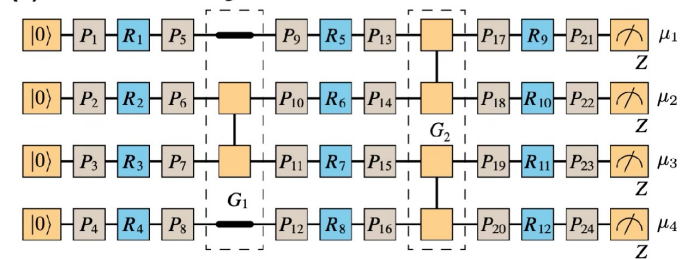
## Learning-Based Quantum Error Mitigation

Armands Strikis<sup>1,\*</sup> Dayue Qin<sup>2,†</sup> Yan Zhu Chen<sup>3,4</sup> Simon C. Benjamin,<sup>1</sup> and Ying Li<sup>2,\*</sup>

(a) Circuit without error mitigation

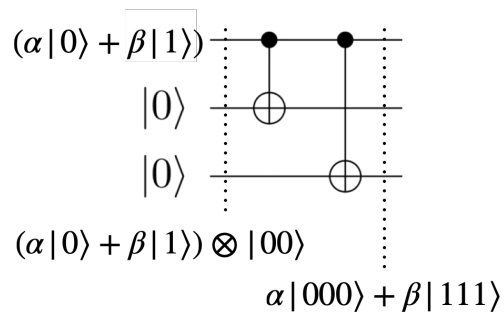


(b) Circuit with error mitigation

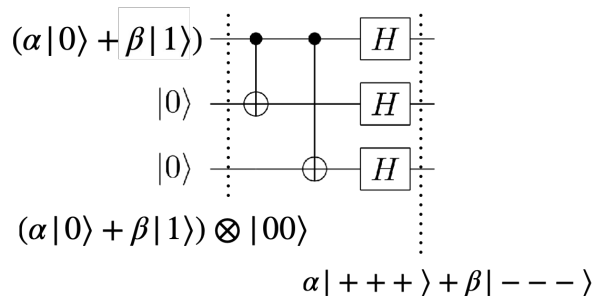


# Long term: error correction

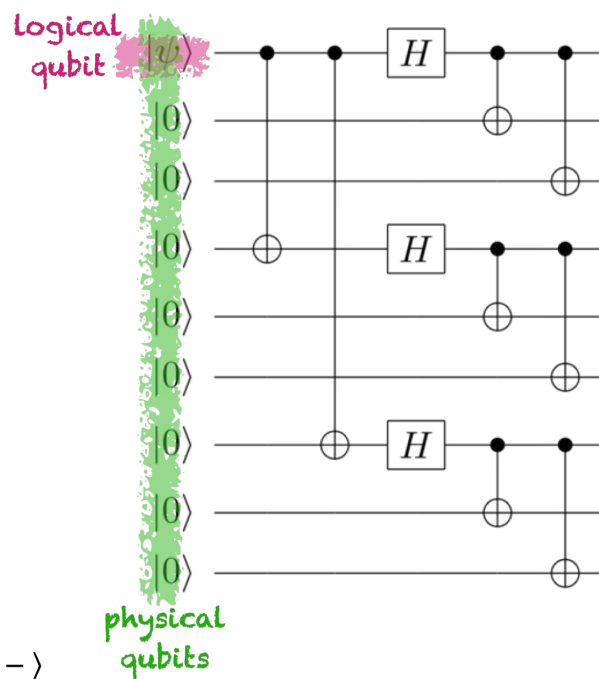
## BIT FLIP



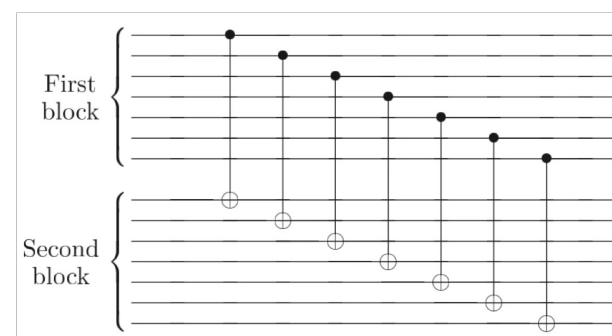
## PHASE FLIP



## BIT+PHASE: SHOR CODE



## FAULT-TOLERANCE

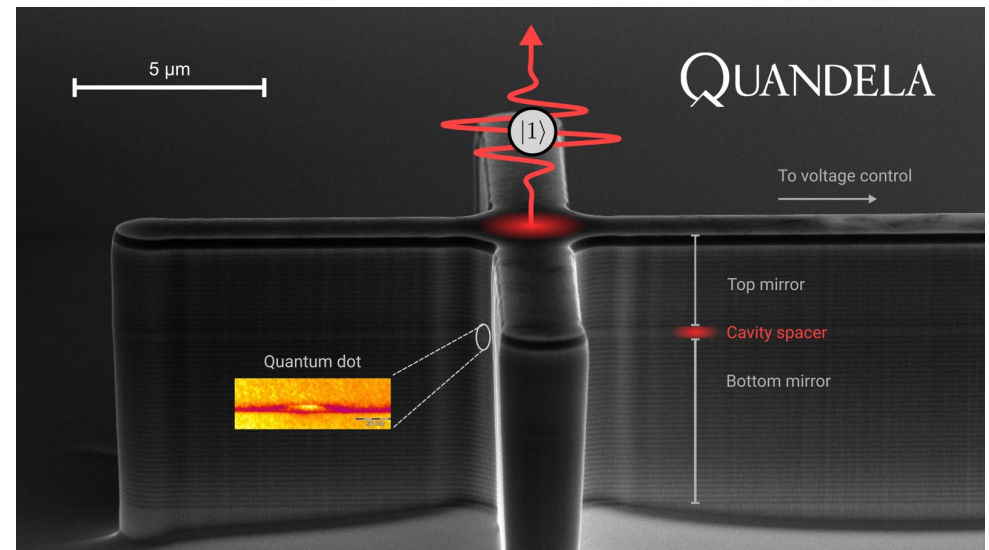
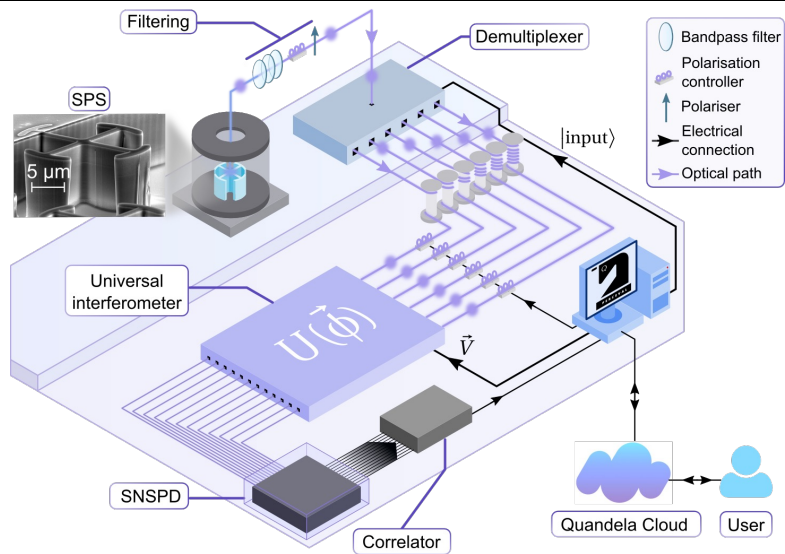


## THRESHOLD THEOREM

**The threshold theorem:** Provided the noise in individual quantum gates is below a certain constant threshold and obeys certain physically reasonable assumptions, it is possible to reliably perform an arbitrarily long quantum computation, with only a small overhead in the size of the circuit necessary to ensure reliability.



# And what about Quandela?



# If you want to go deeper in quantum information

## Quantum Computing in the NISQ era and beyond

John Preskill

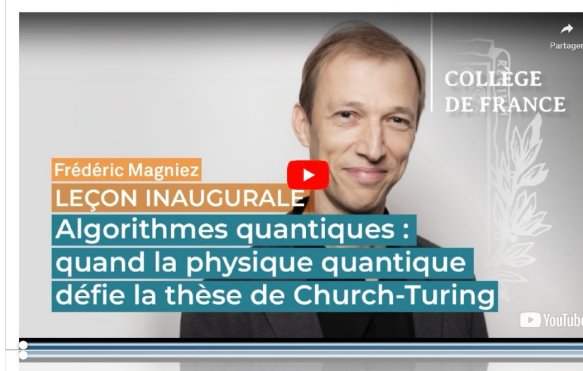
Institute for Quantum Information and Matter and Walter Burke Institute for Theoretical Physics,  
California Institute of Technology, Pasadena CA 91125, USA  
30 July 2018

## Introduction to Quantum Information Science Lecture Notes

Scott Aaronson<sup>1</sup>

## Lecture Notes for Physics 229: Quantum Information and Computation

John Preskill  
California Institute of Technology



Frédéric Magniez  
Cours, séminaires, colloques  
Informatique et sciences numériques

La chaire

Biographie et publications

Cours, séminaires, colloques

Actualités

Flux RSS Podcast

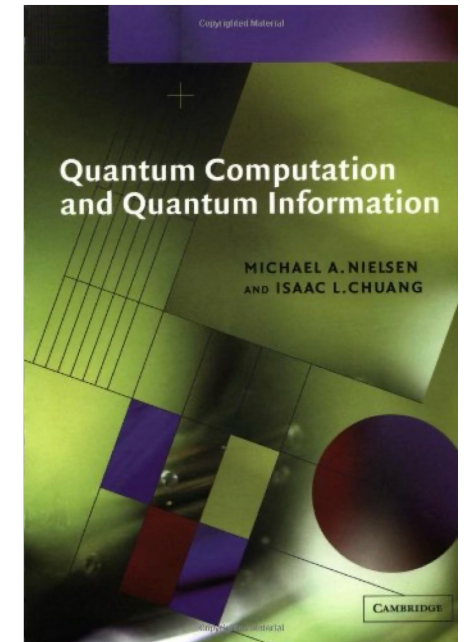
Tout Cours Séminaire Colloque Leçon inaugurale

2020 - 2021

07 avr 2021 → 09 juin 2021

Cours  
Frédéric Magniez  
Algorithmes quantiques

Algorithmes quantiques  
Frédéric Magniez





**SEE? THAT WASN'T SO HARD!**

**QUANDELA**

The end

→ [www.quandela.com](http://www.quandela.com)

